TEST-CASE PRIORITIZATION WITH MODEL-CHECKERS

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ABSTRACT
The order in which test-cases are executed has an influence on the rate at which faults can be detected. In this paper we demonstrate how test-case prioritization can be performed with the use of model-checkers. For this, different well known prioritization techniques are adapted for model-based use. New property based prioritization techniques are introduced. In addition it is shown that prioritization can be done at test-case generation time, thus removing the need for test-suite post-processing. Several experiments are used to show the validity of these ideas.

KEY WORDS
Software testing, Test-case prioritization, Model-checker testing, Property testing.

1 Introduction
It has been shown [13] that the order in which the test-cases of a test-suite are executed has an influence on the rate at which faults can be detected. For example, test-cases can be sorted such that a given coverage criterion like statement coverage is reached as fast as possible. While this prioritization of test-cases can increase the rate at which test-cases are detected in the first run, the idea can be extended to include information about cost factors, e.g., the costs of test-case execution or the costs of certain faults that can be detected with certain test-cases [7]. Furthermore, when a test-suite is reused many times for regression testing, information about the version changes can be incorporated [8], and histories of detected faults [11] can be included.

In this paper we demonstrate how test-case prioritization can be performed with the use of model-checkers. As common prioritization techniques are based on program source-code, these techniques have to be adapted to the model-based setting. In addition, new property based prioritization techniques made possible by the use of model-checkers are introduced.

Obviously, a model-checker based method to test-case prioritization is a useful addition to model-checker based test-case approaches. We therefore show how prioritization can be done at test-case generation time when using model-checkers to create test-cases. That way, no post-processing of the test-suites is necessary while still achieving an improved fault detection ratio of the resulting test-suite. The ideas described in this paper are illustrated using several example applications.

This paper is organized as follows: Section 2 recalls the principles of test-case prioritization and presents different prioritization techniques for model-based use. Then, Section 3 describes how prioritization is performed with the help of a model-checker, while Section 4 shows how prioritization can be done at test-case creation time. Section 5 describes our experiment setup and presents the results achieved. Finally, Section 6 concludes the paper.

2 Test-Case Prioritization
In this section the ideas of test-case prioritization are recalled, and techniques for prioritization are presented.

2.1 Preliminaries
Test-case prioritization is the task of finding an ordering of the test-cases of a given test-suite such that a given goal is reached faster. The test-case prioritization problem is defined by Rothermel et al. [13] as follows:

Given: $T$, a test-suite; $PT$, the set of permutations of $T$; $f$ a function from $PT$ to the real numbers.

Problem: Find $T' \in PT$ such that $(\forall T'' \in PT)(T'' \neq T')[f(T') \geq f(T'')]$.

$PT$ is the set of all possible orderings of $T$, and $f$ is a function that yields an award value for any given ordering it is applied to. $f$ represents the goal of the prioritization. For example, the goal might be to reach a certain coverage criterion as fast as possible, or to improve the rate at which faults are detected. There are different test-case prioritization techniques that can be used to achieve such goals.

2.2 Test-Case Prioritization Techniques
Several different prioritization methods have been discussed in previous works [13, 8]. These methods are gen-

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erally based on the source code of a program, e.g., the coverage of statements or functions. In contrast, when using a model-checker to determine prioritization we base the techniques on a functional model of the program to test. This section does not provide a complete overview of all available prioritization techniques but selects a representative subset that can be used to illustrate the usefulness of model-checkers in the prioritization process. In addition, the use of a model-checker allows new kinds of prioritization techniques which are introduced in this section.

**Total Coverage Prioritization:** There are several code-based prioritization methods that sort test-cases by the number of statements or functions they cover. Model-checker based testing allows the formulation of coverage criteria as properties, as described in the next section. We therefore generalize from different code based methods to a coverage based method which is applicable to any coverage criterion expressible as a set of properties.

For example, the model-based coverage criterion *Transition Coverage* requires that each transition in an automaton is executed at least once. Test-case prioritization according to transition coverage sorts test-cases by the number of different transitions executed.

**Additional Coverage Prioritization:** Total Coverage Prioritization achieves that those test-cases with the biggest coverage are executed first. This does not necessarily guarantee that the coverage criterion is achieved as fast as possible. Additional coverage prioritization first picks the test-case with the greatest coverage, and then successively adds those test-cases that cover the most yet uncovered parts.

**Total FEP Prioritization:** This technique orders test-cases by the ability to expose faults (fault-exposing-potential). Mutation analysis [6] is used to determine these values. For a given program a set of mutants is created by the application of a set of mutation operators. Each application of a mutation operator creates a mutant of the source code that differs from the original by a single valid syntactic change. The mutation score represents the ratio of mutants that a test-suite can distinguish from the original program. This mutation score can be calculated for each test-case separately, and then used as an award value for test-case prioritization. Total FEP prioritization uses the mutation score for a total sorting.

**Additional FEP Prioritization:** Similarly to additional coverage based prioritization test-cases can be sorted by the number of additional, yet undetected mutants. First the test-case with the highest mutation score is chosen, and then successively those test-cases are added that maximize the total number of detected mutants. Traditionally, this FEP based prioritization is computationally more complex than coverage based methods.

**Total Property Prioritization:** This is a new technique made possible by the use of model-checkers. It is based on the idea of *property relevance* [9]. A test-case consists of values that are used as input data for the system under test, i.e., they represent the inputs the system receives from its environment. A test-case is said to be relevant to a requirement property if a property violation is possible when the input values are provided to an erroneous implementation. In practice, this can be determined by checking whether there is a mutant that can violate the property. A test-case can of course be relevant to more than one property. Total property prioritization sorts test-cases by the number of properties they are relevant to.

**Additional Property Prioritization:** Similarly to the previous techniques, this method begins with the test-case that is relevant to the most properties and then successively adds test-cases that are relevant to yet uncovered properties.

**Hybrid Property and Coverage Prioritization:** If the number of properties is significantly smaller than the number of test-cases, then a property based prioritization can quickly achieve property coverage. In general, the prioritization of the remaining test-cases starts again with the test-case with the highest award value. However, it is also conceivable to combine two different award functions. For example, it can be useful to sort test-cases totally based on the number of relevant properties, and then use a coverage prioritization as a secondary sorting method within test-cases of equal property relevance. We use transition coverage as secondary award value in our experiments.

**Random Prioritization:** Random prioritization is interesting for evaluation of the different techniques. In average, any sorting method should achieve better results than random prioritization in order to be useful. We therefore use random prioritization as a lower bound for our analysis.

**Optimal Prioritization:** The optimal prioritization sorts test-cases such that a given set of faults is detected with the minimum number of test-cases. This technique is not applicable in practice as it requires a-priori knowledge about the faults that are to be exposed. However, in experiments with known mutants it serves as upper bound for improvements that can be achieved with prioritization.

### 3 Determining Prioritization with Model-Checkers

In this section we show how the prioritization methods presented in the previous section can be performed in practice. As mentioned, we use model-checkers for prioritization. In order to do so it is necessary to re-formulate test-cases as models, which allows analysis with regard to certain properties. This can be easily done by basing the transition relation of all variables on a special state-counting
variable, as suggested by Ammann and Black [1]. As an example, assume a simple test-case \( t = \{(x = 1, y = 0), (x = 0, y = 1), (x = 1, y = 1)\} \). Using the input language of the model-checker NuSMV [5] which we used for our experiments, the test-case can be expressed as:

\[
\begin{align*}
\text{MODULE} & \quad \text{main} \\
\text{VAR} & \quad \text{init} (y) := 0; \\
& \quad \text{next} (y) := \text{case} \\
& \quad \text{if} \quad \text{x} : \text{boolean}; \\
& \quad \text{y} : \text{boolean}; \\
& \quad \text{State} \geq 0..2; \\
\text{ASSIGN} & \quad \text{init} (\text{x}) := 1; \\
& \quad \text{init} (\text{State}) := 0; \\
& \quad \text{next} (\text{State}) := \text{case} \\
& \quad \text{if} \quad \text{State} = 0; \\
& \quad \text{State} = 1; \\
& \quad \text{State} = 2; \\
& \quad \text{esac}; \\
& \quad \text{if} \quad \text{next} (\text{State}) \neq \text{State} + 1; \\
& \quad \text{esac};
\end{align*}
\]

### 3.1 Coverage Prioritization

Model-based coverage criteria can be expressed as trap properties [10]. For each coverable item one such property is formulated, expressing that the item cannot be reached. For example, a trap property might claim that a certain state is never reached or that a certain transition is never taken. Challenging a model-checker with a model and a trap property results in a counter-example, which is a trace illustrating how the item described by the trap property is reached. This principle is used for test-case creation, where it automatically results in test-suites that achieve a given coverage criterion. It is also used to measure the coverage of test-suites. The test-cases are converted to models as described above, and then the model-checker is challenged with the resulting models and the trap properties. For each trap property that results in a counter-example it is known that the test-case covers the according item.

While for overall coverage measurement it is sufficient to check how many trap properties are violated, this can easily be extended such that each test-case is checked against all trap properties. That way the overall coverage of each test-case can be determined. This information can be used in order to sort test-cases according to their coverage, either totally or additionally. The prioritization works as follows:

1. Create models from test-cases
2. Create trap properties \( TP \) from coverage criterion
3. For each test-case model \( t \) do
   1. Model-check \( t \) against \( TP \)
   2. Each trap resulting in a counter-example is covered
4. Sort test-cases by number of covered traps

### 3.2 FEP Prioritization

Fault exposing prioritization is based on mutation analysis. Model and specification mutation was introduced by Ammann and Black [1]. The ability to expose faults can be measured as the mutation score of a test-case.

With model-checkers, this can be done in two ways. One option is to create mutants of a given model, and then symbolically execute the test-cases against these models by combining the mutant model and the test-case model, using the test-case values as input-values for the mutant. A mutant is detected if the model-checker returns a counter-example when queried whether the output values of mutant and test-case are equal along the test-case. Unlike coverage based methods, this requires the model-checker to use the actual model in addition to the test-case model. If the model is complex, then this process is less efficient than the coverage based method.

The alternative is to reflect the transition relation of the model as special properties [4]. Each reflected property refers to one variable. For each possible transition a variable can take, there is one such property. It consists of the transition condition and makes an assertion about the value of the variable in the next state. These reflected properties can then be mutated instead of the original model. When checked against the original model the mutated properties result in efficient test-suites [2]. A mutation score can be efficiently calculated by checking these properties against the test-case models. This prioritization is therefore identical to coverage based prioritization apart from the use of mutated reflected properties instead of trap properties.

### 3.3 Property Prioritization

Property prioritization uses the concept of property relevance. A test-case is relevant to a property if the execution of the test-case can theoretically lead to a violation of the property. As presented in [9], property relevance can be determined with the aid of a model-checker by symbolically executing the test-case against a modified model which is allowed to take one single erroneous transition. The model-checker then efficiently determines if a single erroneous transition is sufficient in order to reach a property violating state during the test-case execution. This process has to be repeated for each test-case.

1. Create modified model \( M' \) from model \( M \)
2. Create models from test-cases
3. For each test-case model \( t \) do
   1. Combine \( t \) and \( M' \) such that \( M' \) takes input values from \( t \) instead of the environment
   2. Model-check \( M' \) against all requirement properties
   3. \( t \) is relevant to each property causing a counter-example
4. Sort test-cases by relevance

While the complexity of this evaluation process can be higher than for coverage or reflection based methods,
it is only necessary to challenge the model-checker once with each test-case, so this is still significantly more efficient than the determination of the mutation score using symbolic execution would be. Once the property relevance of each test-case has been determined, this information can be used in order to calculate a total or adding prioritization for the test-cases.

3.4 Optimal Prioritization

The optimal execution order of a test-suite with regard to a set of mutants is calculated with a greedy algorithm that successively adds the test-case next that detects the most yet undetected mutants.

4 Prioritizing Test-Cases at Creation Time

When creating test-cases automatically it is often the case that redundant test-cases are created. If a new test-case is a prefix of another test-case it is sufficient to retain the subsuming, longer test-case. If a new test-case subsumes other test-cases it is sufficient to retain the new test-case. Redundant test-cases are usually discarded. However, this redundancy information can also be used to prioritize test-cases. If a test-case or part of it is created more than once, this can be seen as an indication that this test-case is more important than other test-cases. With this information prioritization can be performed without post-processing of the test-suite.

Each test-case is assigned an importance value, initially 1. If a test-case is a prefix of another test-case or equal to it, the importance of this other test-case is increased. If a test-case subsumes other test-cases, then its importance is the sum of the subsumed test-cases plus 1:

1: while \( t = \text{create next test-case} \) do
2: importance of \( t = 1 \)
3: if \( \exists t' \in T \setminus t = t' \) then
4: increase importance of \( t' \) by 1
5: else if \( \exists t' \in T : t \subset t' \) then
6: increase importance of \( t' \) by 1
7: else if \( \exists t' \in T : t \supset t' \) then
8: for all \( t' \in T : t \supset t' \) do
9: replace \( t' \) with \( t \) in \( T \)
10: increase importance of \( t \) with importance of \( t' \)
11: end for
12: else
13: insert \( t \) in \( T \)
14: end if
15: end while
16: sort test-cases by importance

Applied to coverage-based test-case generation using a model-checker, the resulting sorting represents a total sorting by the number of covered traps. Similarly, when using a reflection-based approach the sorting is based on the number of mutants. However, the sorting is not necessarily identical to that resulting from a dedicated analysis, as test-cases can still cover more traps or mutants.

5 Empirical Results

This section presents the results of an empirical evaluation aiming to show that model-based test-case prioritization results in a noticeable performance improvement. We also want to analyze the newly defined property coverage techniques in comparison to well-known techniques. Finally we want to determine whether prioritization at test-case generation time results in a measurable improvement.

5.1 APFD

In order to quantify the efficiency gains achieved with a certain test-case prioritization, the metric APFD was introduced by Rothermel et al. [13]. This metric is the weighted average percentage of faults detected over the life of a test-suite. The APFD of a test-suite \( T \) consisting \( n \) test-cases and \( m \) mutants is defined as:

\[
APFD = 1 - \frac{T F_1 + T F_2 + \ldots + T F_m}{nm} + \frac{1}{nm}
\]

Here, \( T F_i \) is the first test-case in ordering \( T' \) of \( T \) which reveals fault \( i \). We use this metric in order to compare the different prioritization techniques.

5.2 Experiment Setup

The evaluation is based on a set of three examples. Each example consists of an SMV-model and specification. Different model-checker based methods (various coverage criteria, different mutation operators, property based methods) are used in order to create 23 different test-suites for each model. For each model a set of mutants is created. Unlike for program mutation, a model-checker can efficiently determine whether a model mutant is equivalent to the original or not. The APFD values for each of the test-suites is calculated using the subset of the inequivalent model mutants that can be detected by the test-suite. Table 1 sums up the results of the test-case generation and the numbers of detected mutants. Only detectable mutants are relevant for the determination of the APFD value, as the test-case execution order has no influence on undetectable mutants. Car Control (CA) is a simplified model of a car control. The Safety Injection System (SIS) example was introduced in [3] and has since been used frequently for studying automated test-case generation. Cruise Control (CC) is based on [12]. In order to validate the method we also use a set of 25 erroneous mutant implementations for the Cruise Control example applications written by Jeff Offutt.

<table>
<thead>
<tr>
<th>Example</th>
<th>CA</th>
<th>SIS</th>
<th>CC</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Avg</td>
<td>Max</td>
<td>Avg</td>
</tr>
<tr>
<td>Test-Cases</td>
<td>51</td>
<td>243</td>
<td>22</td>
</tr>
<tr>
<td>Mutants</td>
<td>264</td>
<td>311</td>
<td>265</td>
</tr>
</tbody>
</table>

Table 1. Test-Suite statistics
5.3 Results

Following the tradition of previous papers about test-case prioritization we use box-plots to illustrate the results of the APFD analysis. The box-plots illustrate minimum, maximum, median and standard deviation for each of the used prioritization methods. As can be seen in Figures 1, 3 and 4, there is still a gap between all prioritization techniques and the optimal prioritization. However, there is an improvement clearly visible compared to the random sorting of the test-cases and the original sorting, as provided by the test-case generation algorithm. Figure 6 lists the average APFD values for all examples and methods in a concise manner. The improvement is not always as significant as reported in previous works. This is probably because we used test-suites of different sizes, and the improvement is not quite so obvious for large test-suites. In general, a large amount of the mutants is detected with the first couple of test-cases (Figure 5), yet the remaining test-cases and mutants can distort the APFD value, if there are many test-cases. Nevertheless, an improvement is visible. Figure 2 illustrates the APFD values for the same test-suites (except the optimal one) as in Figure 1, executed with the 25 erroneous implementations of Cruise Control. The values are comparable and we conclude that model-based prioritization is also valid for real implementations.

![Figure 1. APFD of Cruise Control model](image1)

![Figure 2. APFD of Cruise Control implementation](image2)

![Figure 3. APFD of Safety Injection System](image3)

The prioritization performed at test-case generation time (labeled *presorted* in the figures) is clearly better than random ordering, however there is still a gap between presorted test-suites and post-processing prioritization. This gap is also visible in Figure 5. Interestingly, the presorted test-suites performed better than most other prioritization techniques during the evaluation on the cruise control implementations. In general we can conclude that prioritization at test-case generation is definitely useful, especially as it only requires negligible additional computational costs.

There are only minor differences between the various prioritization techniques. In general, those techniques that use adding sorting perform slightly better than those with total sorting. Property prioritization performs good (regard also Figure 5), in fact it sometimes outperforms coverage based prioritization techniques. However, this case study does not reflect on the quality of the specification. It is conceivable that a specification consisting of more and better properties will result in better property based prioritization.

While model-checkers in general are prone to performance problems this is not a problem for prioritization, as the state space of test-case models is usually significantly smaller than that of related functional models.

6 Conclusion

In this paper we have demonstrated how model-checkers can be used for test-case prioritization. This makes it possible to efficiently apply prioritization when creating test-cases with model-checkers. We adapted several well-known prioritization methods originally based on source-code to models. In addition we introduced new property-based prioritization methods. Finally, we showed that test-case prioritization can be performed automatically during test-case generation, without post-processing.

The experiments described in this paper showed the applicability of test-case prioritization to model-checker based testing. However, in these experiments many factors were not yet included. For example, the actual test-case ex-
execution costs, the costs of potential faults, the fault histories during regression testing or the importance or criticality of requirement properties could be used to optimize test-case prioritization. Weighting factors can easily be included in the prioritization process, as illustrated in [8]. The property based prioritization techniques introduced in this paper also open up new possibilities for combination with approaches that assign different cost measures to properties [14].

References


